



# VK Multimedia Information Systems

Mathias Lux, [mlux@itec.uni-klu.ac.at](mailto:mlux@itec.uni-klu.ac.at)

Dienstags, 16.00 Uhr s.t., E.1.42



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# Selection of Project B

<http://www.uni-klu.ac.at>

- Find a project that
  - ... is personally interesting for you
  - ... you can finish in time (40-60h)
  - ... has something to do with the course
- Opportunities
  - Try before buy: Thesis, etc.
  - Get some work done (for you, employer, ...)
  - Be creative
  - Contribute to open source

# Sample Projects (not to choose)

- LSA of MP3s ID3v2
  - Clustering & retrieval based on metadata
- Java based video summarization
  - Greedy keyframe distance maximization
- Image mosaics
  - Based on LIRe,  
now part of it



# Indexing



- Spatial Indexes
- MDS – FastMap
- Locality Sensitive Hashing
- Metric Indexes
- Inverted Lists



# Indexing Visual Information



- Text is indexed in inverted lists
  - Search time depends on # of terms
- Visual information expressed by “vectors”
  - Combined with a metric capturing the semantics of similarity
  - Inverted list does not work here
  - An “index of vectors” is needed

# Indexing Visual Information

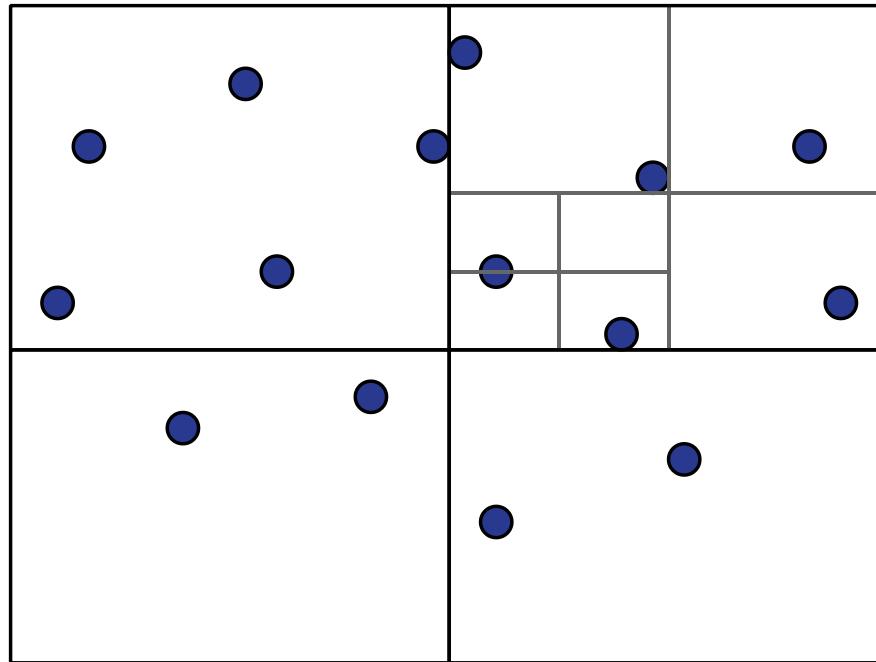


- Vectors describe “points in a space”
  - Space is n-dimensional
  - n might be rather big
- Distance (metric) between points
  - E.g. L1 or L2 ...
- Query is also a vector := point
  - Searching for points (vectors) near to query
- Idea for index:
  - Index neighborhood ...

# Spatial Indexes



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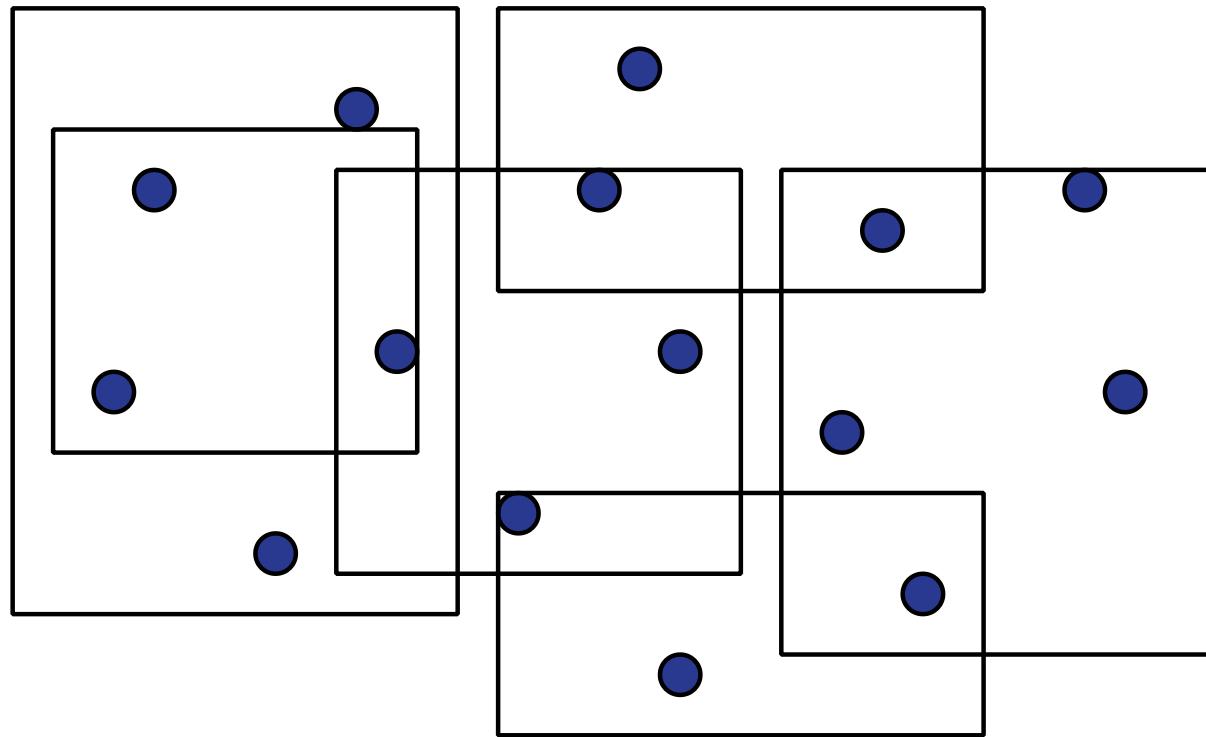


Using equally sized rectangles (Optimal for L1 ...)

# Spatial Indexes



<http://www.uni-klu.ac.at>



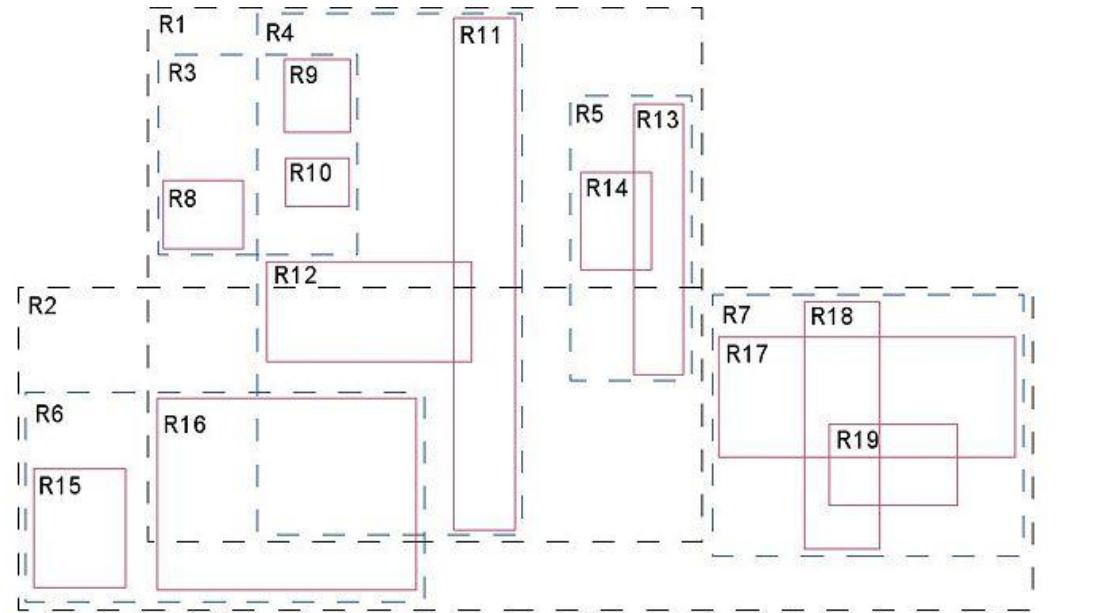
Using overlapping rectangles ...

# Spatial Indexes



- Common data structures
  - R Tree
    - R\*, R+, ....
    - Overlapping rectangles
    - Search is a rectangle
  - Quadtree (Octtree)
    - Equally sized regions, subdivided
    - 4 quadrants or 8 octants
    - Search selects quadrants

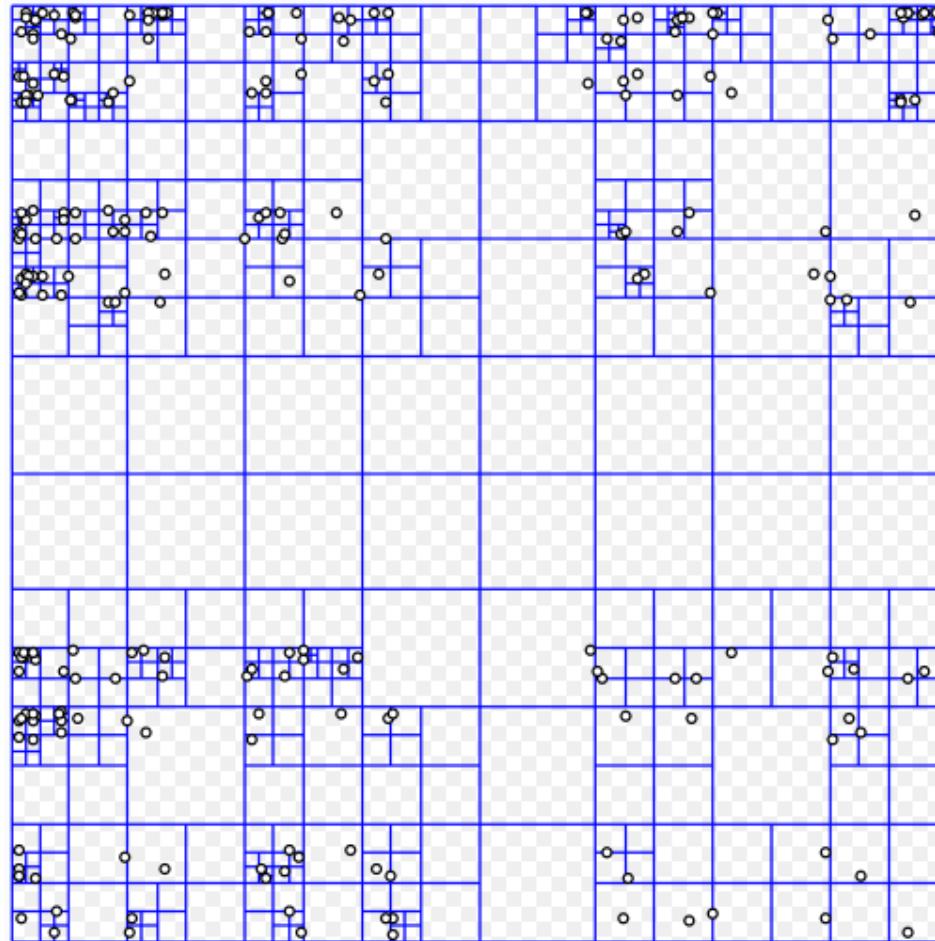
# R-Tree



# Quadtree



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# Spatial Indexes: Drawbacks



- Data structures must minimize
  - false negatives (-> maximizes recall)
  - false positives (-> search time)
- Features, distance function & parameters need to be selected at index time
  - Search combining multiple descriptors is complicated issue
- Works best for spaces with small dimension  $n$ 
  - MDS has to be applied ...

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# Multidimensional Scaling (MDS)



- Reducing the dimensions of a feature space
  - E.g. From 64 dimensions to 8
  - Without loosing too much information about neighborhoods
- Applications in multimedia retrieval
  - Indexing based on coordinates
  - Spatial Indexes:
    - Data structures to find nearest neighbors fast

# Multidimensional Scaling (MDS)



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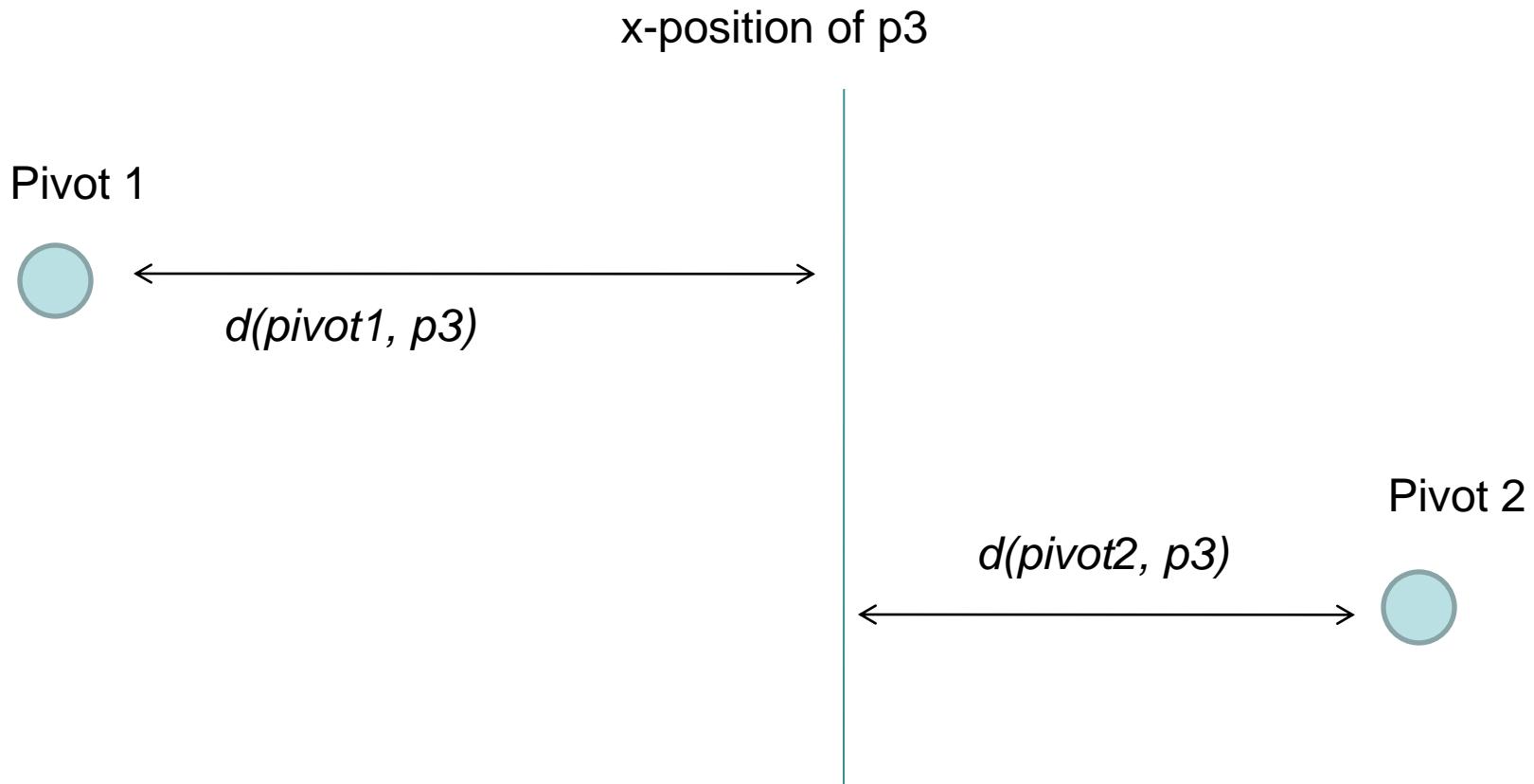
- Interpolation: FastMap
  - Linear in terms of objects
  - Used e.g. in IBM QBIC
- Iterative: Force Directed Placement
  - Iterative optimization of initial placement
  - Cubic runtime

# FastMap

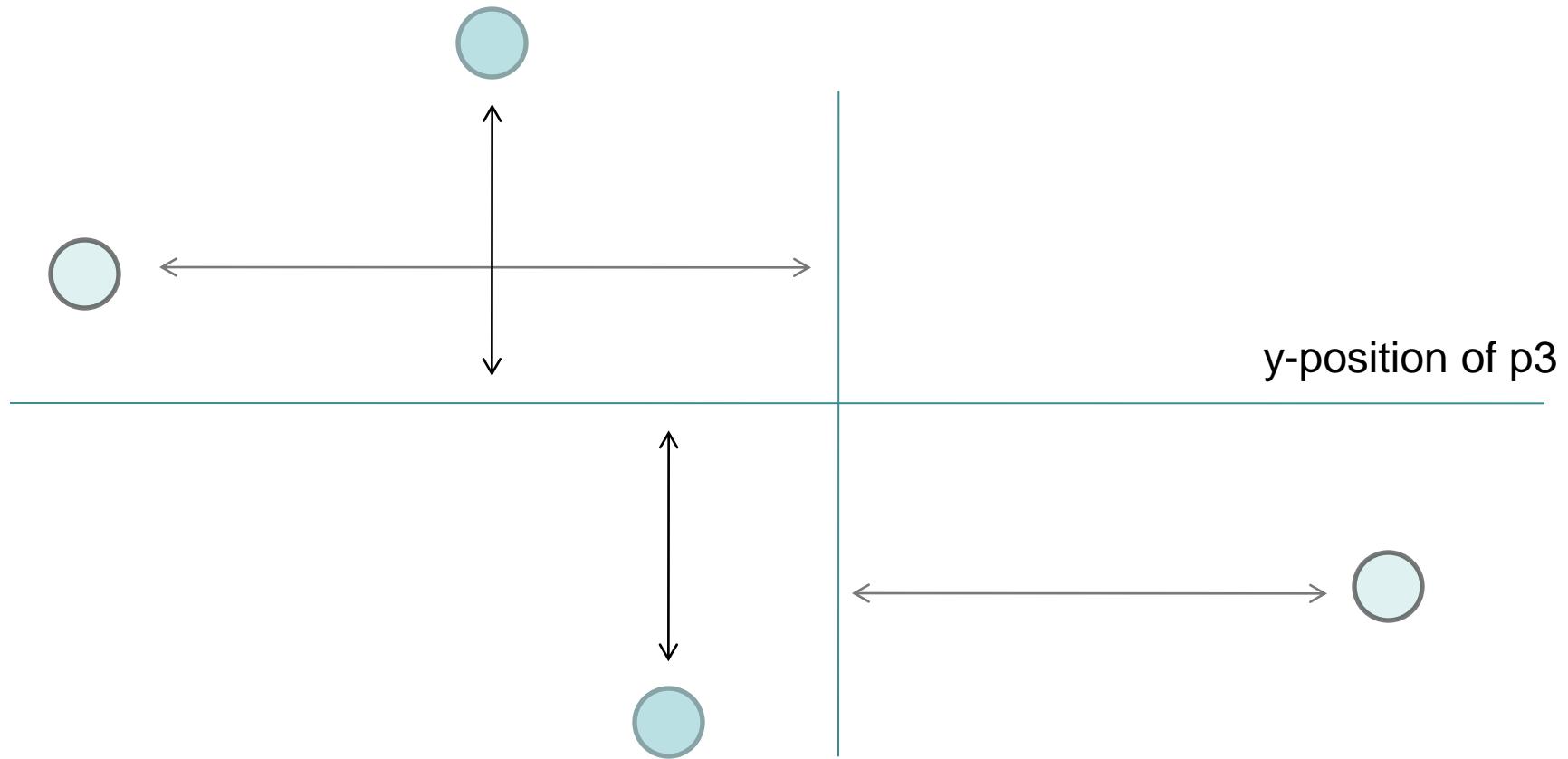


- For Each dimension d
  - Find Pivots (the most distant objects)
  - For each object, which is not a pivot
    - Interpolate position between pivots in this dimension
    - Next object
- Next Pivot

# FastMap



# FastMap



# FastMap: Pivots

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# How to find optimal pivots?



<http://www.uni-klu.ac.at>

- Select one object randomly ->  $P_1$
- Select Object  $P_2$  with maximum distance from  $P_1$  to  $P_2$
- If  $d(P_1, P_2) < t$ 
  - Set  $P_1 = P_2$
  - Goto (2)

Normally no threshold is used but this is done x times.

# Force Directed Placement



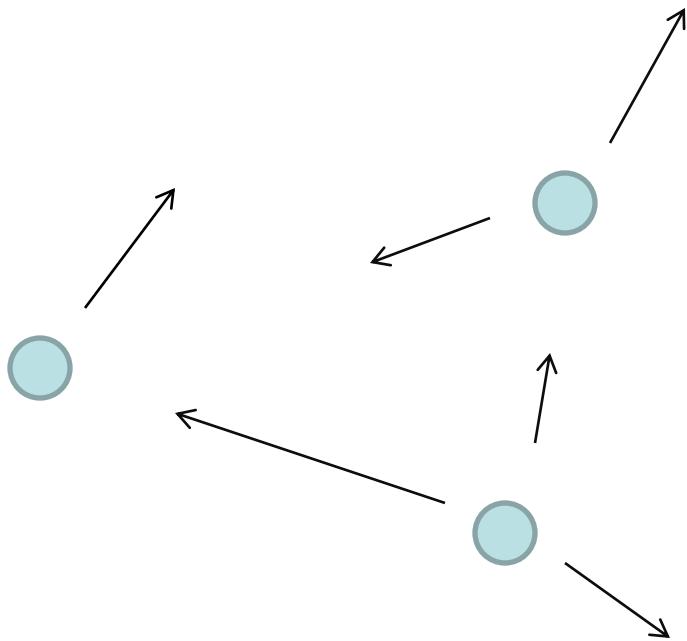
<http://www.uni-klu.ac.at>

1. All objects are assigned coordinates
2. For each object  $o$ 
  - Movement vector  $v = 0$
  - For each object  $p$ 
    - Calculate repulsion & attraction forces between  $o$  &  $p$
    - Compute movement vector  $v(o, p)$  depending on the forces
    - $v = v + v(o, p)$
3. If overall movement is still high goto 2.

# FDP: Parameters



- Gravity as overall attraction
  - Prevents uncontrolled spread
- Overall repulsion
  - Prevents coming objects from coming too close
- Minimum distance
  - If objects are on the coordinates
- Spring parameters
  - Repulsion stronger close up
  - Attraction stronger if far away



# Demo



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- Emir

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# Locality Sensitive Hashing (LSH)

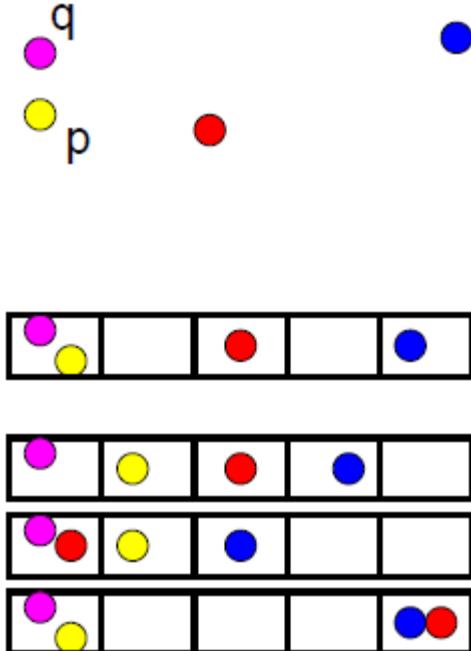


- Algorithm to determine the “Approximate Near(est) Neighbor”
- Given: a set  $P$  of points in  $R^d$
- Nearest Neighbor: query  $q$  returns point  $p \in P$  minimizing  $|p-q|$
- r-Near Neighbor: query  $q$  returns point  $p \in P$  so that  $|p-q| \leq r$

src. <http://people.csail.mit.edu/indyk/mmds.pdf>

# LSH - Idea

- Construct hash functions  $g:R^d \rightarrow U$  so that
  - If  $|p-q| \leq r$  then  $\Pr[g(p)=g(q)]$  is “not so small”
  - If  $|p-q| > cr$  then  $\Pr[g(p)=g(q)]$  is “small”



# LSH - Process

- A family  $H$  of hash functions  $h: \mathbb{R}^d \rightarrow U$  is called  $(P1, P2, r, cr)$ -sensitive if
  - If  $|p-q| \leq r$  then  $\Pr[h(p)=h(q)] > P1$
  - If  $|p-q| > cr$  then  $\Pr[h(p)=h(q)] < P2$
- LSH uses functions  $g(p) = \langle h_1(p), \dots, h_k(p) \rangle$ 
  - Preprocessing
    - Select functions  $g_1, \dots, g_L$
    - Hash all  $p \in P$  to buckets  $g_1(p), \dots, g_L(p)$
  - Query
    - Retrieve points from buckets  $g_1(q), \dots, g_L(q)$

- LSH solves  $c$ -approximate NN with:
  - Number of hash functions:  $L = n^\rho$ ,  
 $\rho = \log(1/P_1)/\log(1/P_2)$
  - E.g., for the Hamming distance we have  $\rho = 1/c$
  - Constant success probability per query  $q$
- LSH schemes
  - Extending beyond Hamming distance
  - Projection based, etc.

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# Metric Indexes



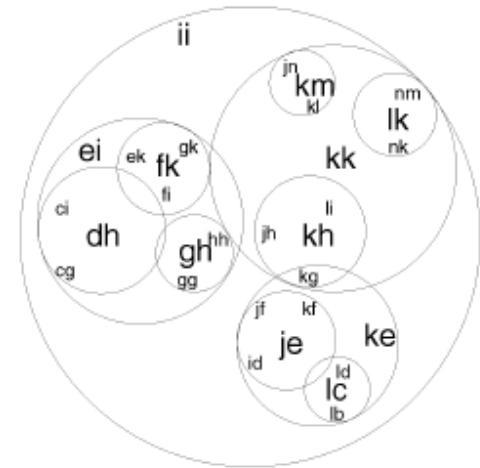
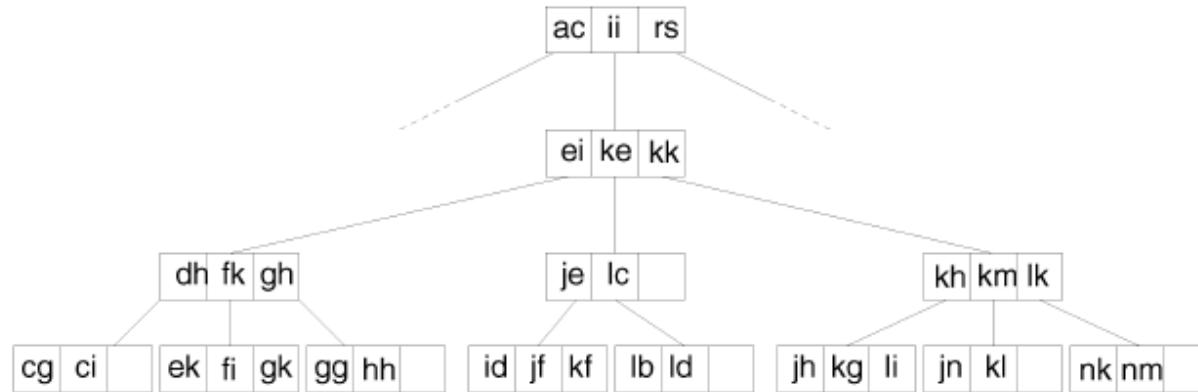
A metric index is a *tree of nodes*

- Each node containing a fixed maximum number of entries
- Each entry is constituted by a routing entry  $D$

src. Berretti, S.; del Bimbo, A. & Vicario, E.  
Efficient Matching and Indexing of Graph Models in Content-Based Retrieval  
*IEEE Transactions on Pattern Analysis and Machine Intelligence*, **2001**, 23, 1089-1105

# Metric Indexes

- $D$  is the root of a sub index in the *covering region* of  $D$ 
  - Also defines a radius  $r_D$  being the maximum distance from  $D$  to any entry in the covering region.

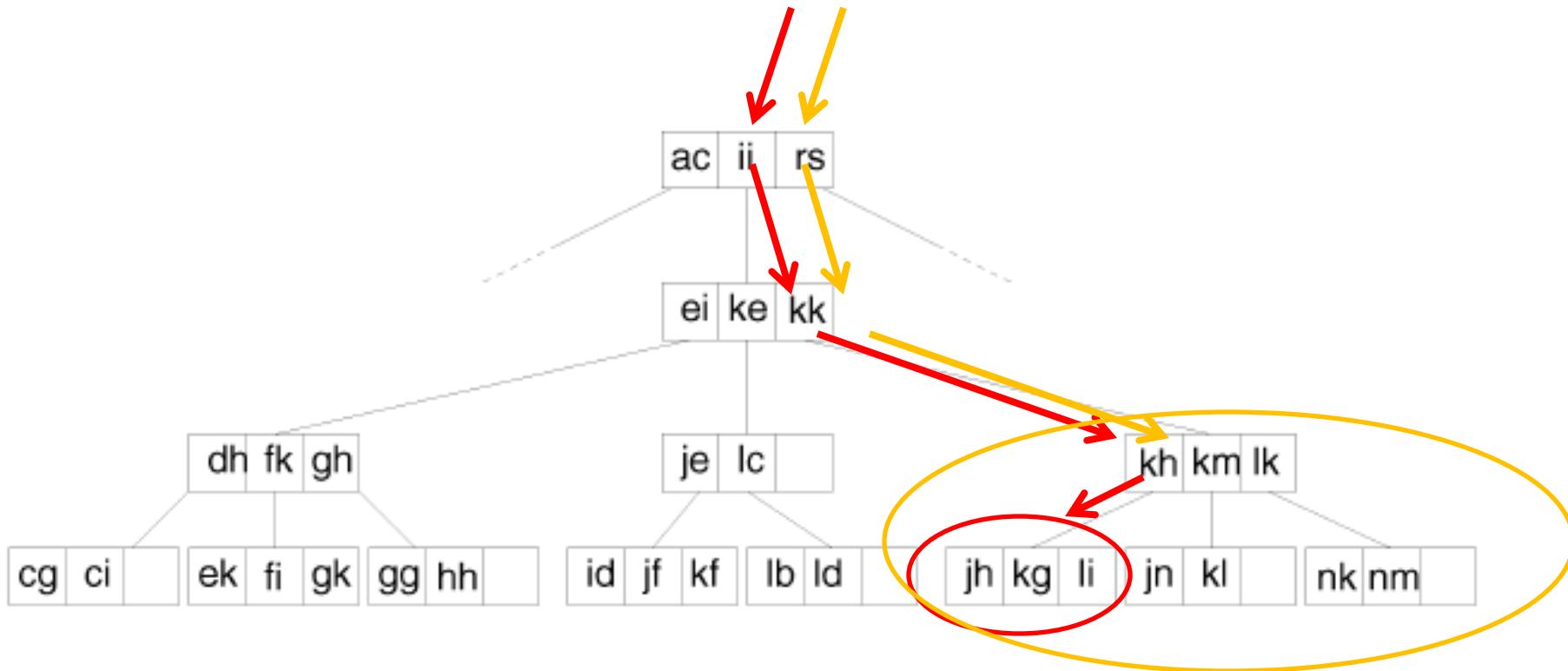


# Metric Index: Construction



- Top-down: Indexing an entire archive at once
  - All documents to index are known
  - No iterative additions
- Bottom-up: Indexing on insertion
  - Documents are indexed as they are added to the collection
  - Optimizations (e.g. splitting) have to be done

# Metric Index: Searching



# Indexing



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# Metric Spaces



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- $\mathcal{M} = (\mathcal{D}, d)$ 
  - Data domain  $\mathcal{D}$
  - *Total (distance) function*  $d: \mathcal{D} \times \mathcal{D} \rightarrow \mathbb{R}$  (metric function or metric)
- The metric space postulates:
  - Non negativity  $\forall x, y \in \mathcal{D}, d(x, y) \geq 0$
  - Symmetry  $\forall x, y \in \mathcal{D}, d(x, y) = d(y, x)$
  - Identity  $\forall x, y \in \mathcal{D}, x = y \Leftrightarrow d(x, y) = 0$
  - Triangle inequality  $\forall x, y, z \in \mathcal{D}, d(x, z) \leq d(x, y) + d(y, z)$

# Similarity Search in Metric Spaces



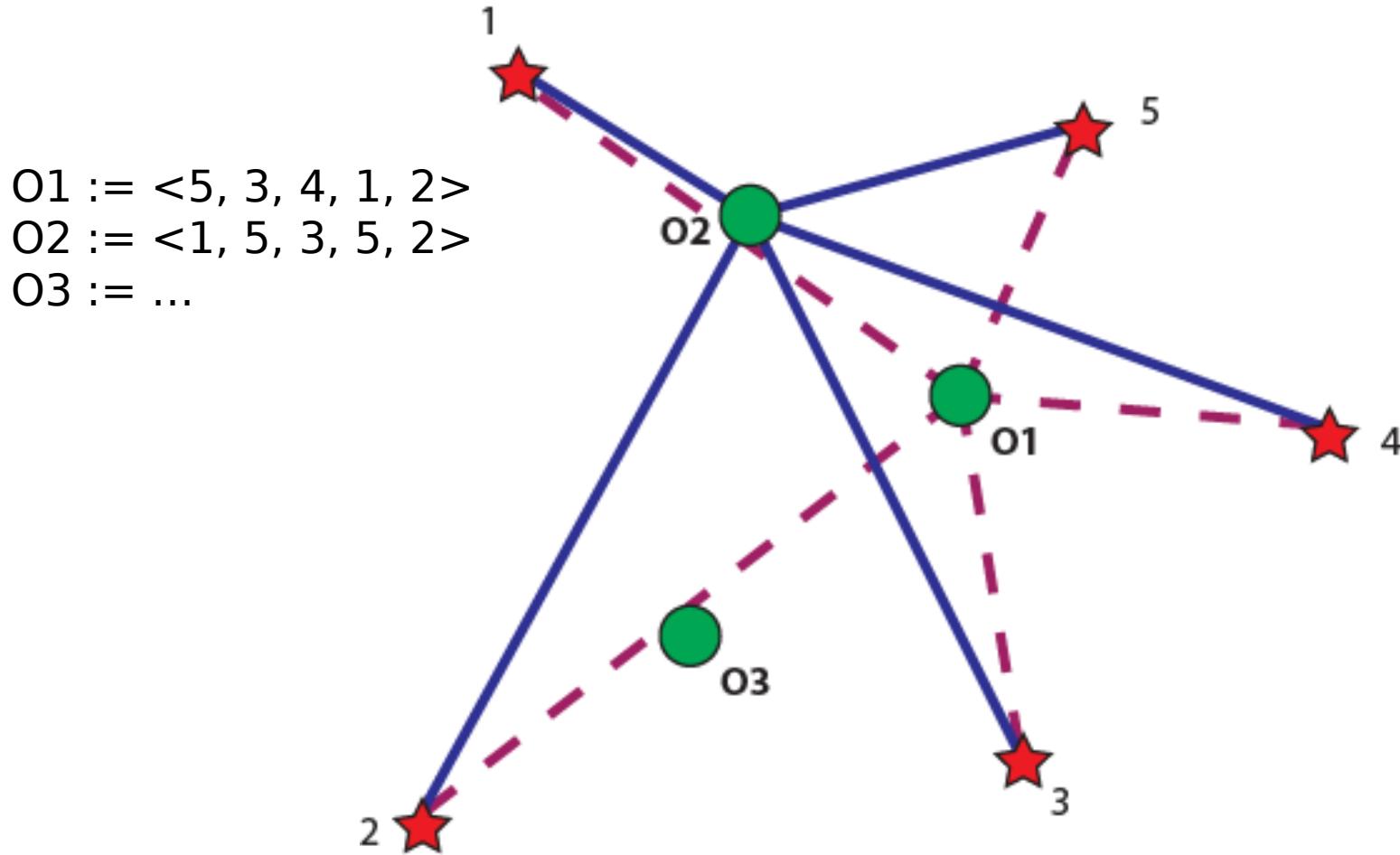
<http://www.uni-klu.ac.at>

- Objects close to one another see the space in a “similar” way
- Choose a set of *reference objects*  $RO$
- Orderings of  $RO$  according to the distances from two similar *data objects* are similar as well
  - Represent every data object  $o$  as an ordering of  $RO$  from  $o$
  - Measure similarity between two data objects by measuring the similarity between the corresponding orderings

# Similarity Search in Metric Spaces



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# Similarity Search in Metric Spaces



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- Spearman Footrule Distance

$$SFD(S_1, S_2) = \sum_{ro \in RO} |S_2(ro) - S_1(ro)|$$

# Similarity Search in Metric Spaces



[Slides G. Amato ...]



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# Thanks ...

- Projekte ?!?