

"Multimedia Information Systems" at Klagenfurt University

Guest Lecture "Social Network Analysis"

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About me

Education:

- 2002 2004
 - PhD. in Knowledge Management, Faculty of Computer Science, TU Graz
- 1997 2002
 - M.Sc., Telematik, TU Graz

Background:

- July 2007 present
 - Ass. Prof. (Univ.Ass.), TU Graz, Austria
- 2006 2007
 - 15 months Post-Doc, University of Toronto, Canada
- 2002 2006
 - Researcher, Know-Center, Austria



Overview

Agenda:

A selection of concepts from Social Network Analysis

- Sociometry, adjacency lists and matrices
- One mode, two mode and affiliation networks
- KNC Plots
- Prominence and Prestige
- Excerpts from Current Research "Social Web"



The Erdös Number

Who was Paul Erdös?

http://www.oakland.edu/enp/

A famous Hungarian Mathematician, 1913-1996 Erdös posed and solved problems in number theory and other areas and founded the field of discrete mathematics.

- 511 co-authors (Erdös number 1)
- ~ 1500 Publications



The Erdös Number

The Erdös Number:

Through how many research collaboration links is an arbitrary scientist connected to Paul Erdös?

What is a research collaboration link? Per definition: Co-authorship on a scientific paper -> Convenient: Amenable to computational analysis

What is my Erdös Number?



me -> S. Easterbrook -> A. Finkelstein -> D. Gabbay -> S. Shelah -> P. Erdös

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- Users
- Listing and
- Tagging goals

A tripartite graph

• User-Tag-Goal





Sociometry as a precursor of (social) network analysis [Wasserman Faust 1994]

- Jacob L. Moreno, 1889 1974
- Psychiatrist,



- born in Bukarest, grew up in Vienna, lived in the US
- Worked for Austrian Government
- Driving research motivation (in the 1930's and 1940's):
 - Exploring the advantages of picturing interpersonal interactions using sociograms, for sets with many actors



Sociometry [Wassermann and Faust 1994]

 Sociometry is the study of positive and negative relations, such as liking/disliking and friends/enemies among a set of people. Can you give an example of web formats that capture such relationships?

FOAF: Friend of a Friend, http://www.foaf-project.org/

XFN: XHTML Friends Network, http://gmpg.org/xfn/

- A social network data set consisting of people and measured affective relations between people is often referred to as a sociometric dataset.
- Relational data is often presented in two-way matrices termed sociomatrices.



Sociometry [Wassermann and Faust 1994]



Fig. 3.2. The six actors and the three sets of directed lines — a multi-variate directed graph

Images Wasserman/Faust page 76 & 82

Table 3.1. Sociomatrices for the six actors and three relations of Figure 3.2

	Frien	dship at	Beginni	ng of Yea	ır		
	Allison	Drew	Eliot	Keith	Ross	Sarah	
Allison	-	1	0	0	1	0	
Drew	0	-	1	0	0	1	
Eliot	0	1	-	0	0	0	Solid lines
Keith	0	0	0	-	1	0	
Ross	0	0	0	0	-	1	
Sarah	0	1	0	0	0	-	
	F	riandshin	at Fnd	of Vear			
	Allison	Drew	Eliot	Keith	Ross	Sarah	
Allison	-	1	0	0	1	0	
Drew	0	-	1	0	1	1	
Eliot	0	0	-	0	1	0	dashed lines
Keith	0	1	0	-	1	0	
Ross	0	0	0	1	-	1	
Sarah	0	1	0	0	0	-	
		Lin	on Maan				
	Allison	Drew	Eliot	Keith	Ross	Sarah	
Allison	-	0	0	0	1	1	
Drew	0	-	1	0	0	0	
Eliot	0	1	-	0	0	0	dotted lines
Keith	0	0	0	-	1	1	
Ross	1	0	0	1	-	1	
Sarah	1	0	0	1	1	-	



How can we represent (social) networks?

We will discuss three basic forms:

- Adjacency lists
- Adjacency matrices
- Incident matrices



Adjacency Matrix (or Sociomatrix)

- Complete description of a graph
- The matrix is symmetric for nondirectional graphs
- A row and a column for each node
- Of size m x n (m rows and n colums)



Adjacency matrices

taken from http://courseweb.sp.cs.cmu.edu/~cs111/applications/ln/lecture18.html





Adjacency lists

taken from http://courseweb.sp.cs.cmu.edu/~cs111/applications/ln/lecture18.html





Incidence Matrix

- (Another) complete description of a graph
- Nodes indexing the rows, lines indexing the columns
- g nodes and L lines, the matrix I is of size g x L
- A "1" indicates that a node n_i is incident with line l_i
- Each column has exactly two 1's in it





Fundamental Concepts in SNA

[Wassermann and Faust 1994]

- Actor
 - Social entities

- Which networks would not qualify as social networks?
- Def: Discrete individual, corporate or collective social units
- Examples: people, departments, agencies
- Relational Tie
 - Social ties

Which relations would not qualify as social relations?

- Examples: Evaluation of one person by another, transfer of resources, association, behavioral interaction, formal relations, biological relationships
- Dyad
 - Emphasizes on a tie between two actors
 - Def: A dyad consists of two actors and a tie between them
 - An inherent property between two actors (not pertaining to a single one)
 - Analysis focuses on dyadic properties
 - Example: Reciprocity, trust



Fundamental Concepts in SNA [Wassermann and Faust 1994]

- Triad
 - Def: A subgroup of three actors and the possible ties among them



- Transitivity
 - If actor i "likes" j, and j "likes" k, then i also "likes" k
- Balance
 - If actor i and j like each other, they should be similar in their evaluation of some k
 - If actor i and j dislike each other, they shold evaluate k differently





Fundamental Concepts in SNA [Wassermann and Faust 1994]

Social Network

- Definition: Consists of a finite set or sets of actors and the relation or relations defined on them
- Focus on relational information, rather than attributes of actors



One and Two Mode Networks

- The mode of a network is the number of sets of entities on which structural variables are measured
- The number of modes refers to the number of distinct kinds of social entities in a network
- One-mode networks study just a single set of actors
- Two mode networks focus on **two sets of actors**, or on **one set of actors** and **one set of events**





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Two Mode Networks

- Example:
- Two types of nodes





Affiliation Networks

- Affiliation networks are two-mode networks
 - Nodes of one type "affiliate" with nodes of the other type (only!)
- Affiliation networks consist of subsets of actors, rather than simply pairs of actors
- Connections among members of one of the modes are based on linkages established through the second
- Affiliation networks allow to study the dual perspectives of the actors and the events





Is this an Affiliation Network? Why/Why not?





Examples of Affiliation Networks on the Web

- Facebook.com users and groups/networks
- XING.com users and groups
- Del.icio.us users and URLs
- Bibsonomy.org users and literature
- Netflix customers and movies
- Amazon customers and books
- Scientific network of authors and articles
- etc



Representing Affiliation Networks As Two Mode Sociomatrices



	Allison	Drew	Eliot	Keith	Ross	Sarah	Party 1	Party 2	Party 3
Allison	-	0	0	0	0	0	1	0	1
Drew	0	-	0	0	0	0	0	ť	0
Eliot	0	0		0	0	0	Ő	1	1
Keith	0	0	0		0	0	Ő	ô	1
Ross	0	0	0	0	-	ŏ	ĩ	ĭ	î
Sarah	0	0	0	0	0		1	î	ò
Party 1	1	0	0	0	1	1	-	0	0
Party 2	0	1	1	0	1	1	0		õ
Party 3	1	0	1	1	1	Ó	õ	0	

Fig. 8.3. Sociomatrix for the bipartite graph of six children and three parties

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Two Mode Networks and One Mode Networks

- **Folding** is the process of transforming two mode networks into one mode networks
- Each two mode network can be folded into 2 one mode networks





Transforming Two Mode Networks into One Mode Networks

•Two one mode (or co-affiliation) networks (folded from the children/party affiliation network)



C...Children P...Party





Transforming Two Mode Networks into

*

'Falksches Schema'						
		-1	0			
	*/+	2	-3			
2	3	4	-9			
1	-7	-15	21			
-2	5	12	-15			

$$\mathbf{M}_{\mathbf{P}} = \mathbf{M}_{\mathbf{PC}} * \mathbf{M}_{\mathbf{PC}}$$

C...Children

P...Party

	Allison	Drew	Eliot	Keith	Ross	Sarah
Party 1	1	0	0	0	1	1
Party 2	0	1	1	0	1	1
Party 3	1	0	1	1	1	0

		Party 1	Party 2	Party 3
	Party 1	3	2	2
=	Party 2	2	4	2
	Party 3	2	2	4

	Party 1	Party 2	Party 3
Allison	1	0	1
Drew	0	1	0
Eliot	0	1	1
Keith	0	0	1
Ross	1	1	1
Sarah	1	1	0



Output: Weighted regular graph

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The k-neighborhood graph, G_k

Given bipartite graph B, users on left, interests on right



The k-neighborhood graph, G_k

Given bipartite graph B, users on left, interests on right



The k-neighborhood graph, G_k

Given bipartite graph B, users on left, interests on right



The k-neighborhood graph, G_k

Given bipartite graph B, users on left, interests on right













The KNC-plot

The k-neighbor connectivity plot

- How many connected components does G_k have?
- What is the size of the largest component?

Answers the question:

how many shared interests are meaningful?

- Communities, Cuts

Analysis

Four graphs:

- LiveJournal
 - Blogging site, users can specify interests
- Y! query logs (interests = queries)
 - Queries issued for Yahoo! Search (Try it at www.yahoo.com)
- Content match (users = web pages, interests = ads)
 - Ads shown on web pages
- Flickr photo tags (users = photos, interests = tags)

All data anonymized, sanitized, downsampled

- Graphs have 100s of thousands to a million users







Centrality and Prestige [Wasserman Faust 1994]

Which actors are the most important or the most prominent in a given social network?

What kind of measures could we use to answer this (or similar questions)?

- What are the implications of directed/undirected social graphs on calculating prominence?
- In directed graphs, we can use Centrality and Prestige
- ⇒ In undirected graphs, we can only use Centrality



Prominence [Wasserman Faust 1994]

We will consider an actor to be prominent if the ties of the actor make the actor particularly visible to the other actors in the network.





Actor Centrality [Wasserman Faust 1994]

Prominent actors are those that are extensively involved in relationships with other actors.

This involvement makes them more visible to the others

No focus on directionality -> what is emphasized is that the actor is involved

A *central actor* is one that is involved in many ties. [cf. Degree of nodes]



Actor Prestige [Wasserman Faust 1994]

- A prestigious actor is an actor who is the object of extensive ties, thus focusing solely on the actor as a recipient.
- [cf. indegree of nodes]

Only quantifiable for directed social graphs.

Also known as status, rank, popularity



Different Types of Centrality in Undirected Social Graphs [Wasserman Faust 1994]

Degree Centrality

- Actor Degree Centrality:
 - Based on degree only

Closeness Centrality

- Actor Closeness Centrality:
 - Based on how close an actor is to all the other actors in the set of actors
 - Central nodes are the nodes that have the shortest paths to all other nodes

Betweeness Centrality

- Actor Betweeness Centrality:
 - An actor is central if it *lies between other actors* on their geodesics
 - The central actor must be between many of the actors via their geodesics



Centrality and Prestige in Undirected Social Graphs [Wasserman Faust 1994]



Fig. 5.1. Three illustrative networks for the study of centrality and prestige

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What cliques can

Cliques, Subgroups [Wasserman Faust 1994]

Definition of a Clique

 A clique in a graph is a maximal complete subgraph of three or more nodes.

Remark:

- Restriction to at least three nodes ensures that dyads are not considered to be cliques
- Definition allows cliques to overlap

Informally:

 A collection of actors in which each actor is adjacent to the other members of the clique



Fig. 7.1. A graph and its cliques



Subgroups [Wasserman Faust 1994]

Cliques are very strict measures

- Absence of a single tie results in the subgroup not being a clique
- Within a clique, all actors are theoretically identical (no internal differentiation)
- Cliques are seldom useful in the analysis of actual social network data because definition is overly strict
- So how can the notion of cliques be extended to make the resulting subgroups more substantively and theoretically interesting?

⇒ Subgroups based on reachability and diameter



Which 2-cliques

can you identify in the following

graph?

n cliques [Wasserman Faust 1994]

N-cliques require that the **geodesic distances** among members of a subgroup **are small** by defining a **cutoff value n** as the maximum length of geodesics connecting pairs of actors within the cohesive subgroup.

An n-clique is a maximal complete subgraph in which the largest geodesic distance between any two nodes is no greater than n.



Fig. 7.2. Graph illustrating n-cliques, n-clans, and n-clubs









Fig. 7.2. Graph illustrating n-cliques, n-clans, and n-clubs

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3 Two-mode networks 352 people want to do this... start running again I want to do this - User-Goal People doing this: - Goal-Tag peaceful24 pepper Popular Tags: San Jose 8 entries - User-Tag 28 entries cardio determination exercise fitness health improvement life personal run running <u>fmiller</u> <u>mcfun</u> Frankfurt am Main Ontario Your Tags: 4 entries 3 entries No tags yet. We have combined information 🚹 Add tags Andilee1976 TrudiChavez Richmond Virginia from the 3 entries 3 entries Sponsored Links Sale: Running User-Goal and Caffiend the fringed one Rund ums Joggen - jetzt günstig bei Davis Perth neckermann.at bestellen & sparen! 2 entries 2 entries www.neckermann.at/Joggen Goal-Tag UK Gear Running Shoes swade val576 Richmond Sonoma Designed with the British Military 2-mode networks to construct The most durable shoes available 2 entries 2 entries www.ukgear.com and study large-scale goal We Have Your Match Here 20 Million Cute Singles Worldwide association graphs - See all 352 people Meet Singles Near your location SinglesClubJapan.info People doing this are also doing these things: Worth Doing learn spanish (again!) 51 out of 51 people (100%) think · Meet everyone in my FOAF. this is worth doing. • Shrink Texas. People who've done this: Entries Started yesterday. - 2 days ago I ran yesterday. Just a half hour on the treadmill, but still. Felt really good. I'll run again today. Yea!

squarepetal 59 entries WORTH DOING!

WORTH DOING!

Rintin35 21 entries

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Constructing Goal Graphs from Search Query Logs

- Analyzing the tripartite graph of Search
 - Consisting of users, explicit intentional queries and tags





Any questions?

Thank you for your attention.